adamjee maths

A-LEVEL MATHS / EDEXCEL / FREE RESOURCES

Tangents and normals

Question paper

5 questions

Exam questions and marking instructions remain credited to their board.

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1 June 2024 - Paper 2 - Q15

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15. The curve C has equation

$$(x + y)^3 = 3x^2 - 3y - 2$$

(a) Find an expression for $\frac{dy}{dx}$ in terms of x and y.

(5)

The point $P(1, 0)$ lies on C.

(b) Show that the normal to C at P has equation

$$y = -2x + 2$$

(2)

(c) Prove that the normal to C at P does **not** meet C again.

You should use algebra for your proof and make your reasoning clear.

(5)

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Question 15 continued

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Question 15 continued

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Question 15 continued

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Question 15 continued

(Total for Question 15 is 12 marks)

TOTAL FOR PAPER IS 100 MARKS

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7. **In this question you must show all stages of your working.**

Solutions relying on calculator technology are not acceptable.

A curve has equation

$$x^3 + 2xy + 3y^2 = 47$$

(a) Find $\frac{dy}{dx}$ in terms of x and y

(4)

The point $P(-2, 5)$ lies on the curve.

(b) Find the equation of the normal to the curve at P, giving your answer in the form $ax + by + c = 0$, where a, b and c are integers to be found.

(3)

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Question 7 continued

(Total for Question 7 is 7 marks)

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7. **In this question you should show all stages of your working.**

Solutions relying entirely on calculator technology are not acceptable.

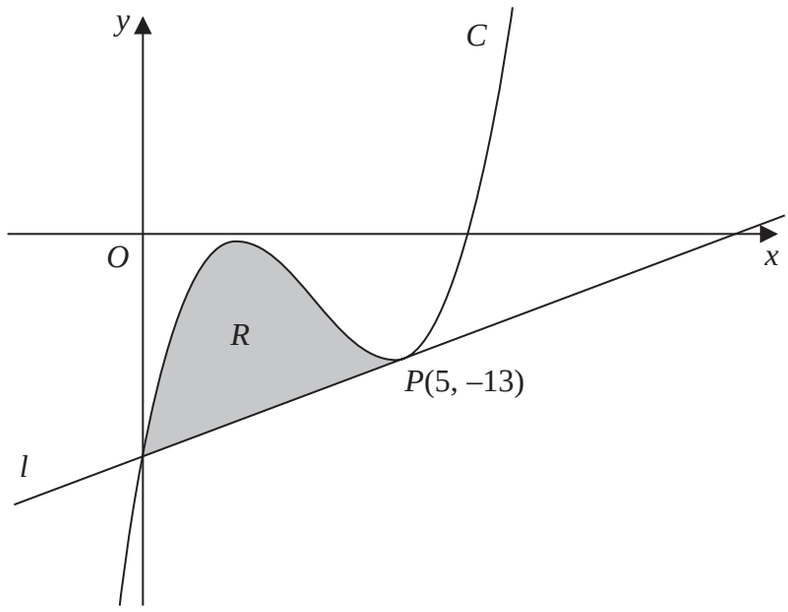


Figure 2

Figure 2 shows a sketch of part of the curve C with equation

$$y = x^3 - 10x^2 + 27x - 23$$

The point $P(5, -13)$ lies on C

The line l is the tangent to C at P

(a) Use differentiation to find the equation of l, giving your answer in the form $y = mx + c$ where m and c are integers to be found.

(4)

(b) Hence verify that l meets C again on the y-axis.

(1)

The finite region R, shown shaded in Figure 2, is bounded by the curve C and the line l.

(c) Use algebraic integration to find the exact area of R.

(4)

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Question 7 continued

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Question 7 continued

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Question 7 continued

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8. The curve C has equation

$$px^3 + qxy + 3y^2 = 26$$

where p and q are constants.

(a) Show that

$$\frac{dy}{dx} = \frac{apx^2 + bqy}{qx + cy}$$

where a, b and c are integers to be found.

(4)

Given that

- the point $P(-1, -4)$ lies on C
- the normal to C at P has equation $19x + 26y + 123 = 0$

(b) find the value of p and the value of q.

(5)

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Question 8 continued

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Question 8 continued

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Question 8 continued

(Total for Question 8 is 9 marks)

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13. The curve C has parametric equations

$$x = \sin 2\theta \qquad y = \text{cosec}^3 \theta \qquad 0 < \theta < \frac{\pi}{2}$$

(a) Find an expression for $\frac{dy}{dx}$ in terms of θ

(3)

(b) Hence find the exact value of the gradient of the tangent to C at the point where $y = 8$

(3)

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Question 13 continued

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